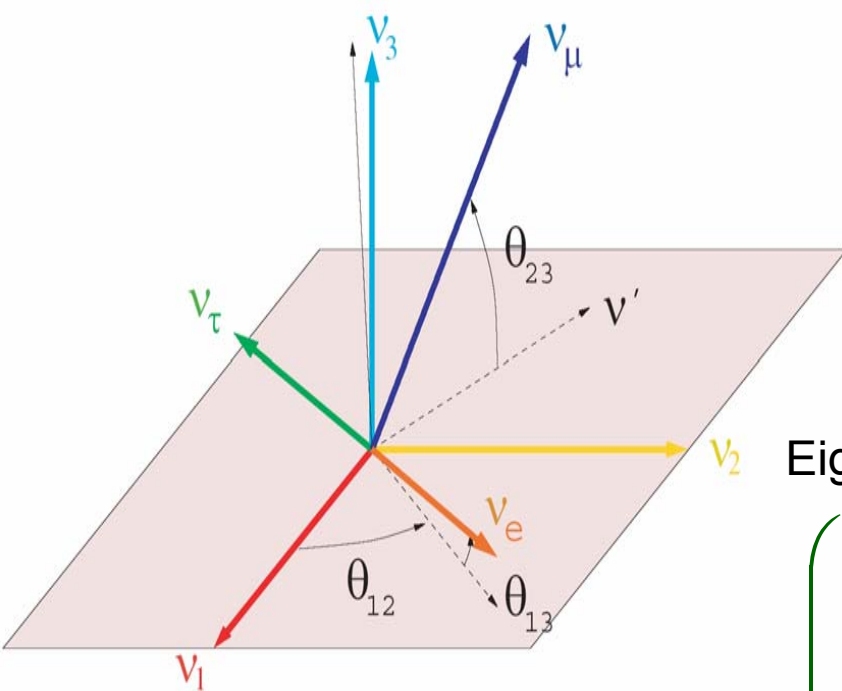


# Off-Axis Physics Overview

H.Sobel  
UCI  
April 16, 2004  
SAGENAP

- There has been a revolution in Neutrino Physics.
  - Observation of Atmospheric Neutrino oscillations (Super-K, Soudan, Macro).
  - Confirmation by K2K.
  - Observation of Solar Neutrino oscillations (Chlorine, Super-K, SAGE, Gallex, SNO)
  - Confirmation by KamLAND

# Three Neutrino Picture

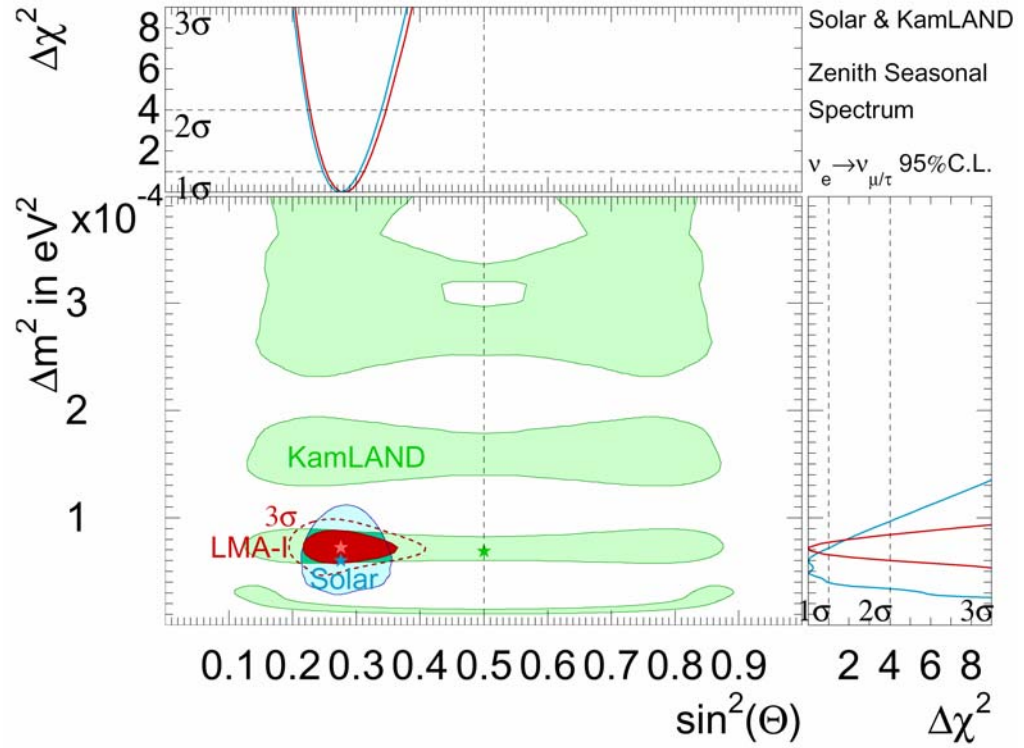
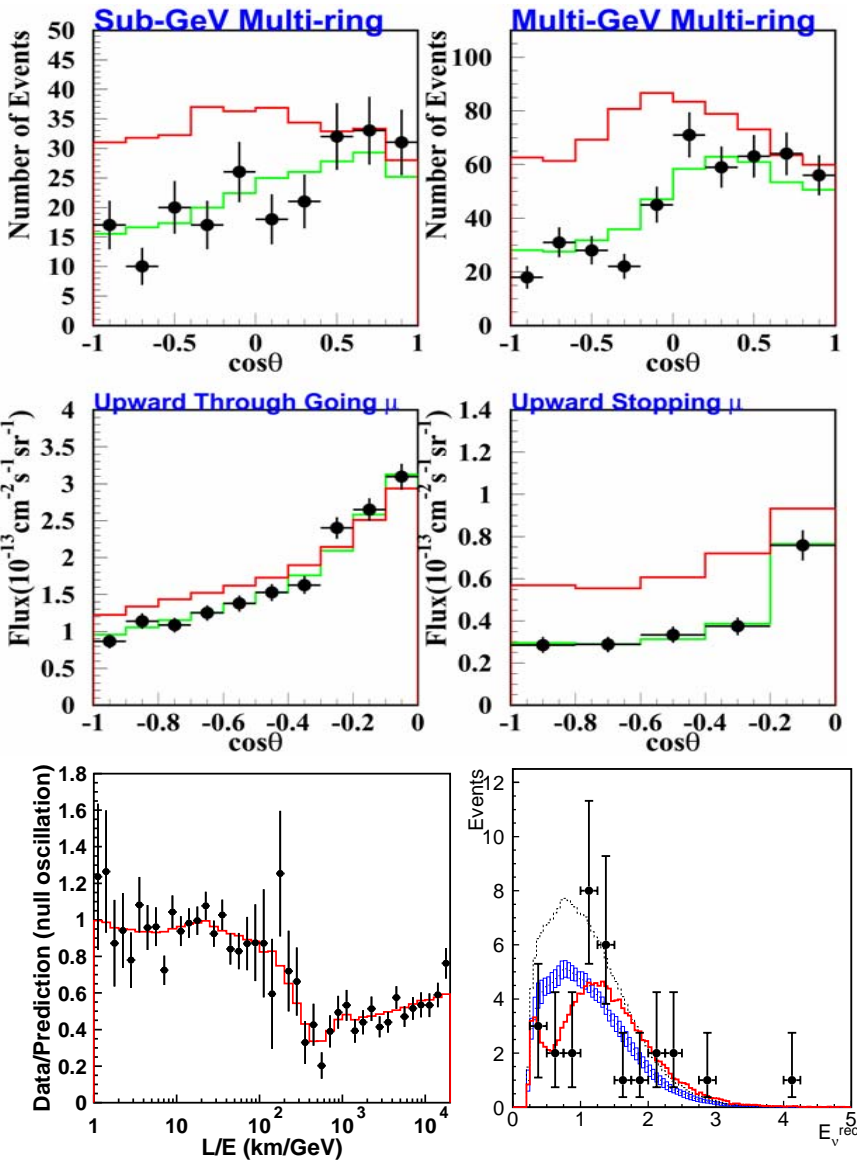


Flavor Eigenstates	MNS Maki-Nakagawa-Sakata mixing matrix	Mass eigenstates
$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$	$= \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}$	$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$

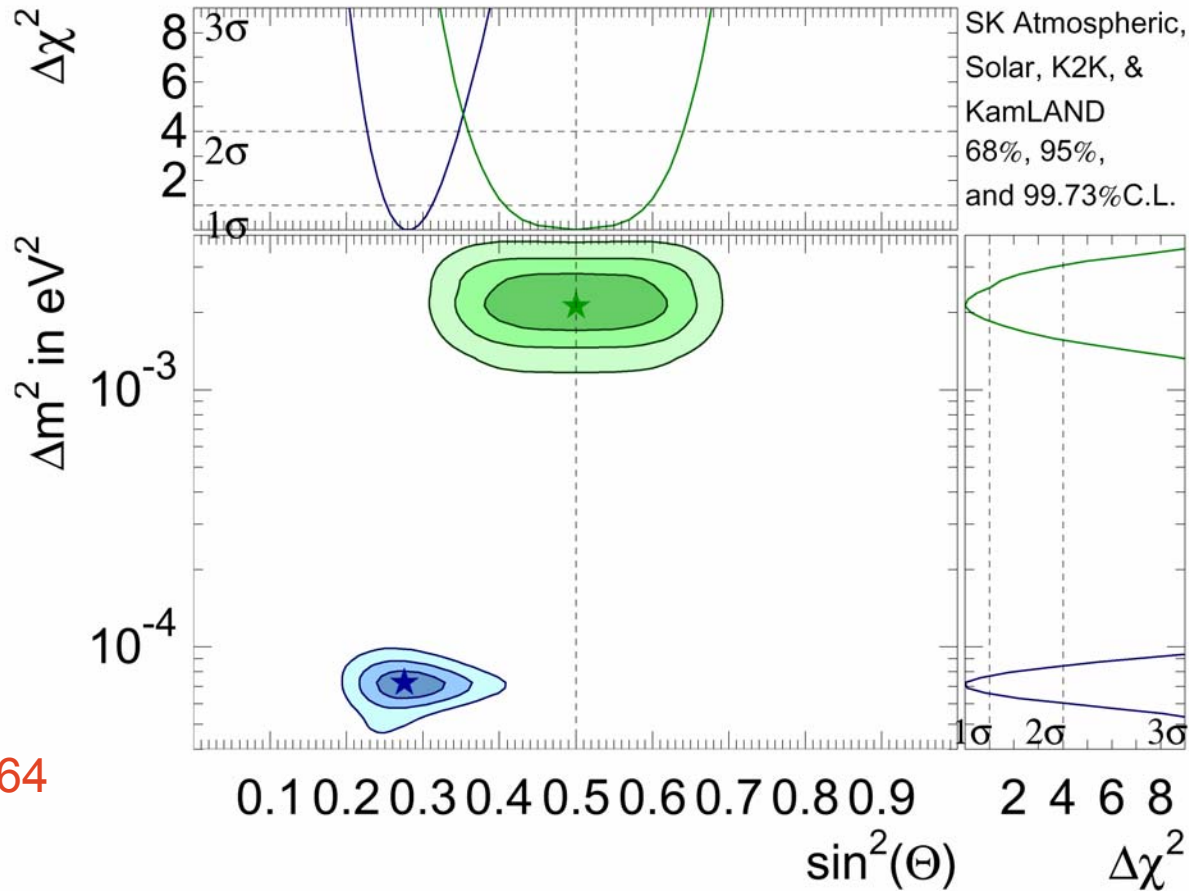
3 independent parameters  
+ 1 complex phase

$\theta_{12}, \theta_{23}, \theta_{13}, \delta$

# Current Results



# Combined analysis



hep-ex/0310064

$$1.6 \times 10^{-3} < \Delta m^2_{\text{ATMOS}} < 2.6 \times 10^{-3} \text{ eV}^2$$

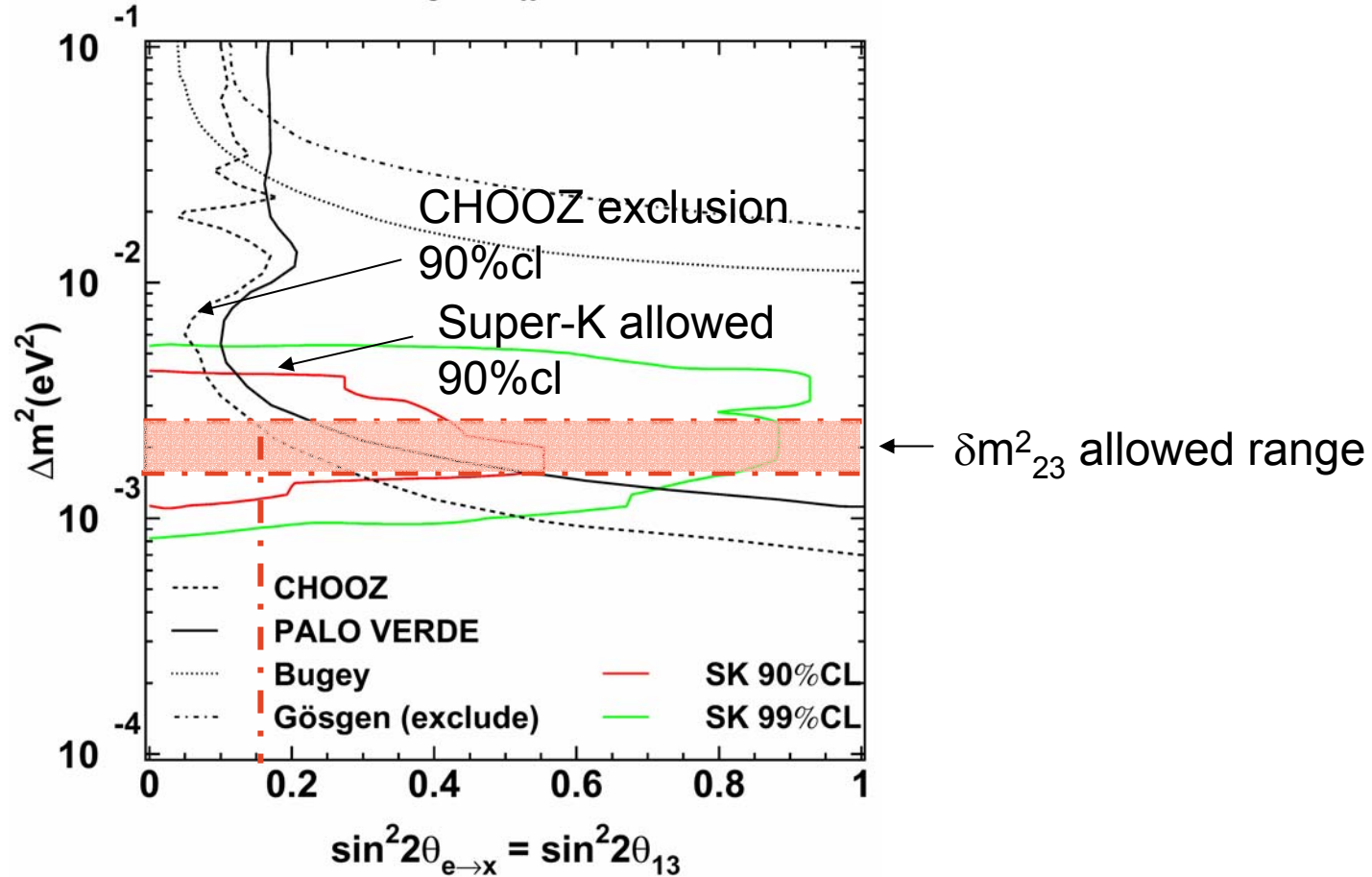
$$\sin^2 2\theta_{23} > 0.91$$

$$6.1 \times 10^{-5} < \Delta m^2_{\text{SOLAR}} < 8.5 \times 10^{-5} \text{ eV}^2$$

$$0.71 < \sin^2 2\theta_{12} < 0.91$$

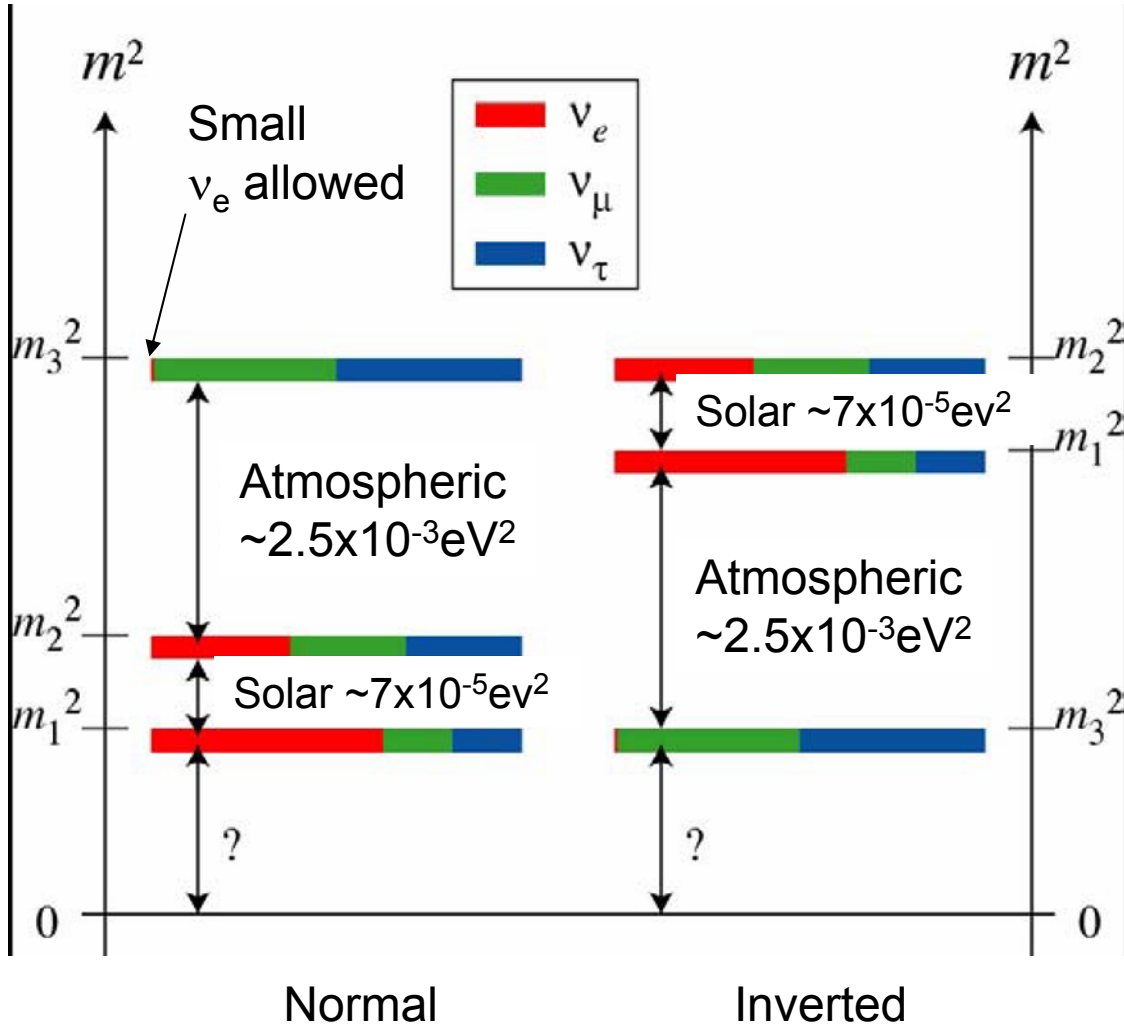
# $\theta_{13}$ Limits

$$\nu_e \leftrightarrow \nu_x$$



**@ $\delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$   $\sin^2 2\theta_{13} < 0.16$  or  $\theta < \sim 11.5^\circ$**

# Mass Hierarchy



# Remaining Questions

- Measurement of  $\theta_{13}$ 
  - Precision measurements of other quantities
- What is the value of Dirac CP phase  $\delta$ ?
- What is the mass hierarchy?
- What is the mass of the lightest neutrino?
- Are neutrinos Majorana particles?
  - If so what are Majorana phases?

# Off-Axis Physics Program

## Initial Goals

- Discover if  $\theta_{13}$  is non-zero by observing  $\nu_e$  appearance
- Attempt to resolve if  $\theta_{23}$  is non-maximal.
- Precisely determine  $\delta m_{23}^2$  ( $\sim 10^{-4}$  eV<sup>2</sup>)

Combination of more than one distance and/or  $\bar{\nu}_e$  running.

- Discovery of non-zero CP phase
- Determination of mass hierarchy

# $\nu_e$ Appearance

$$\begin{aligned}
 P_{vac\pm}[\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)] &= \sin^2 2\theta_{13} s_{23}^2 \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right) && \text{Small, since chose} \\
 &- \frac{1}{2} s_{12}^2 \sin^2 2\theta_{13} s_{23}^2 \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin \left( \frac{\Delta m_{13}^2 L}{2E} \right) && \text{L/E to match ATM} \\
 &+ 2J_r \cos \delta \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin \left( \frac{\Delta m_{13}^2 L}{2E} \right) \\
 &\mp 4J_r \sin \delta \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right),
 \end{aligned}$$

Where  $J_r = c_{12} s_{12} c_{13}^2 s_{13} c_{23} s_{23}$  (Jarlskog factor)

$$\text{So, } P_{vac}(\nu_\mu \rightarrow \nu_e) \sim \sin^2 2\theta_{13} s_{23}^2 \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right)$$

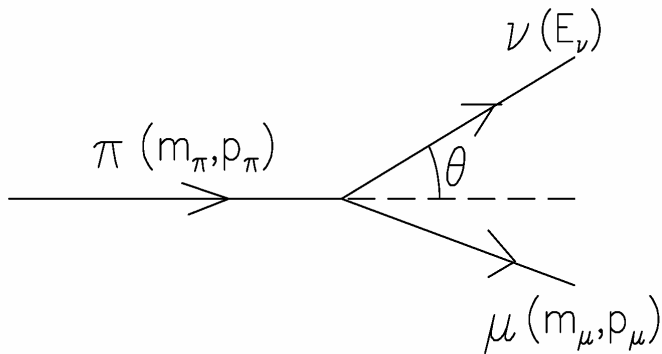
chose E to ~maximize  $\sin^2 \Delta_{ATM}$  at particular location:

- For NOvA: L=820 km  $E_\nu=2.3$  GeV
- For T2K: L=290 km  $E_\nu=600$  MeV

# Off-axis Idea

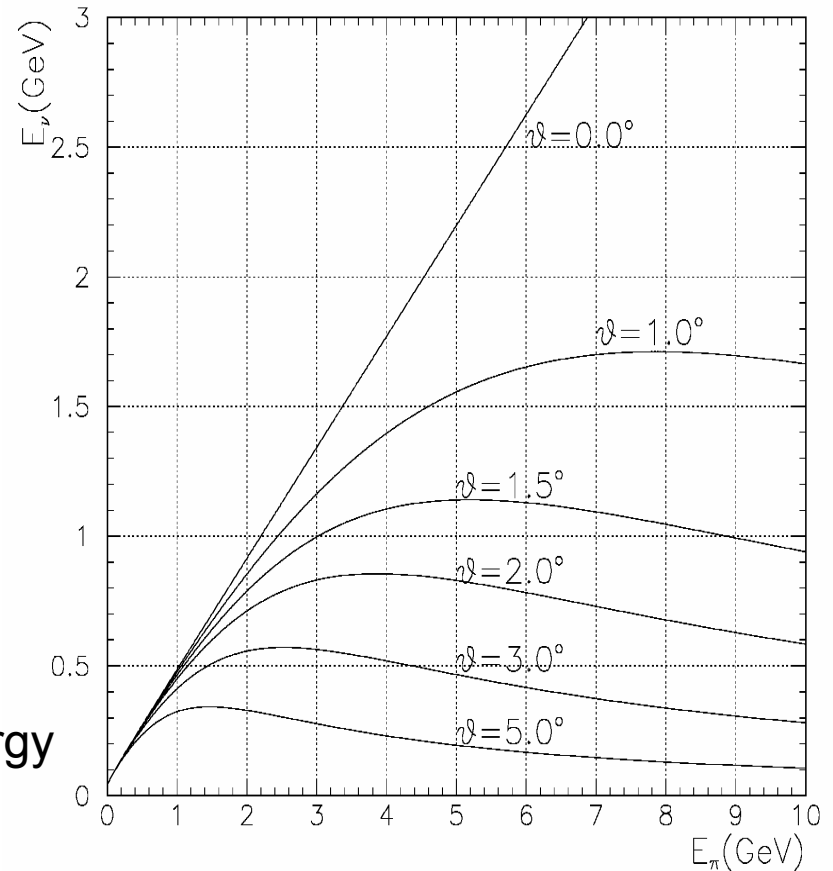
First pointed out in the Long Baseline Neutrino Oscillation Proposal for Experiment, E889, at Brookhaven.)

## Off-axis Kinematics

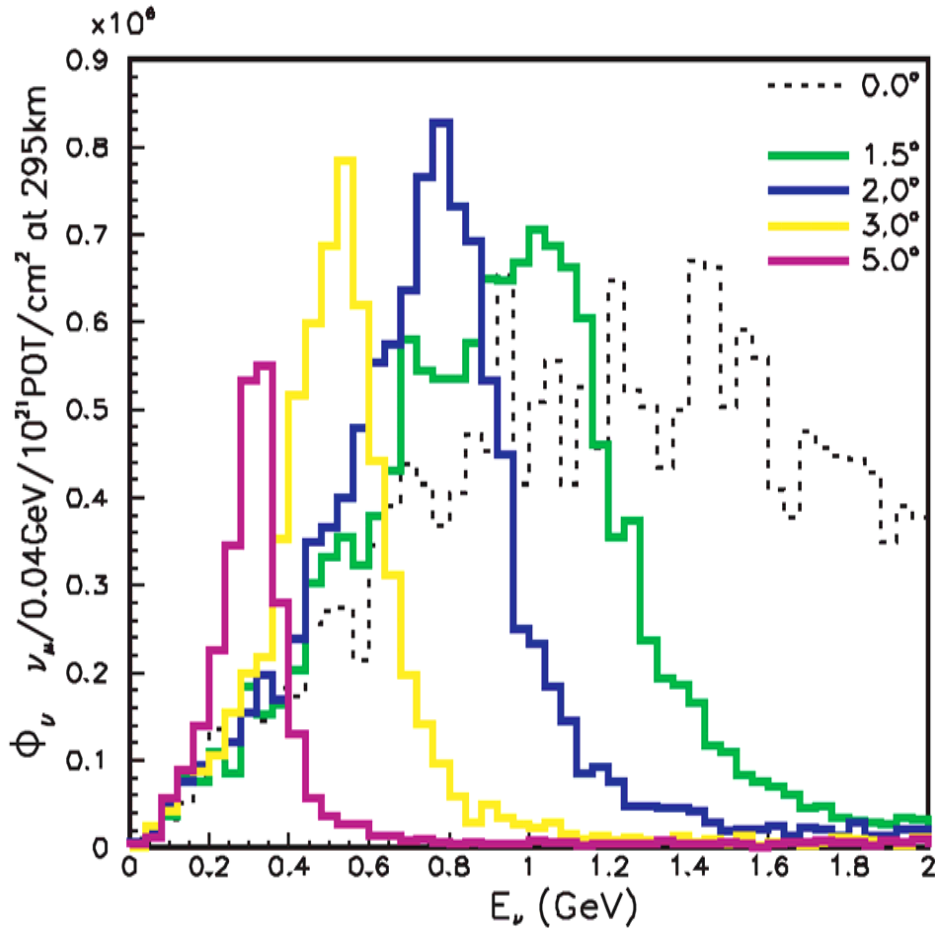


$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2(E_\pi - p_\pi \cos\theta)}$$

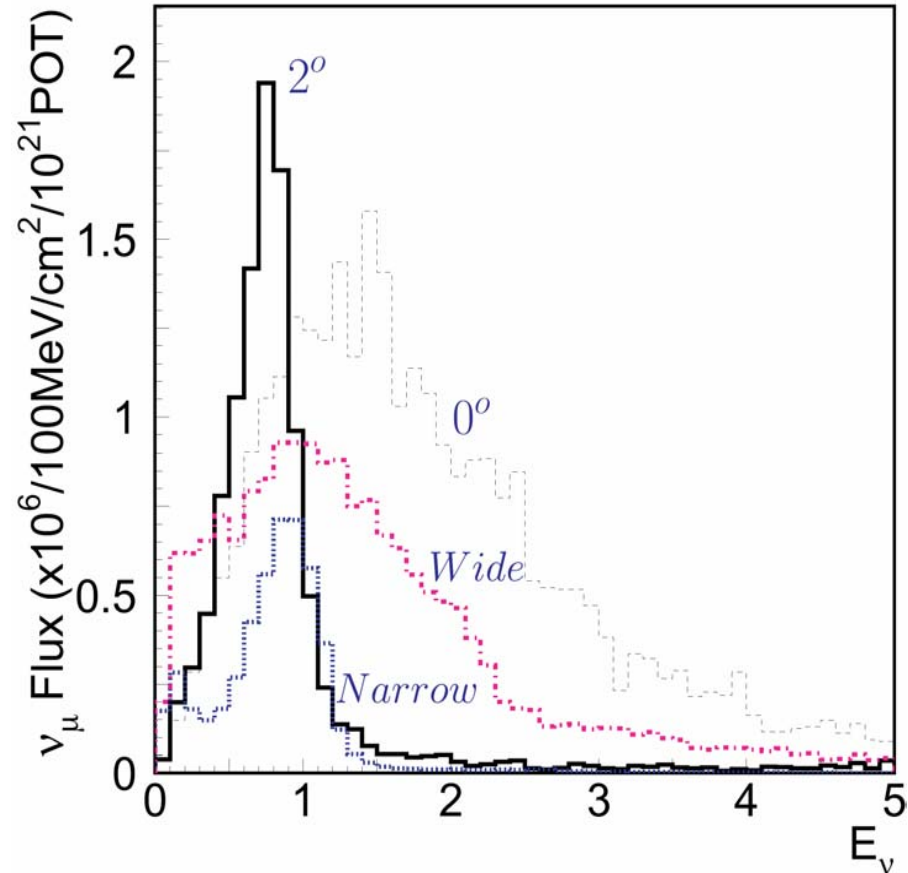
Energy of  $\nu$  relatively independent of  $\pi$  energy



# Pick an Angle $\rightarrow$ Pick an Energy



Energy varies linearly with angle



- Intensity of  $2^\circ$  off-axis beam is higher than  $0^\circ$  wide band.

# High Intensity Proton Accelerators

	Power (MW)	Energy (GeV)	Intensity ( $10^{12}$ ppp)	Rep. rate (Hz)
KEK-PS	0.005	12	6	0.45
AGS	0.14	24	60	0.6
FNAL-MI	0.41	120	40	0.53
SPS	0.3	400	35	0.16
JHF-I	0.77	50	330	0.29
Super-AGS	1.3	28	120	2.5
FNAL-proton driver-I	1.2	16	30	15
SPL	4	2.2	230	50
JHF-II	4	50		

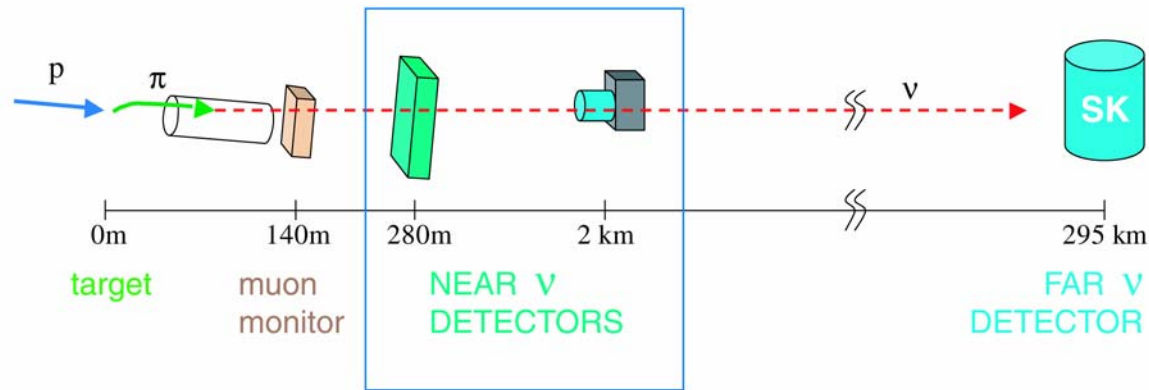
} R&D

# Neutrino Beams

	$\langle E_\nu \rangle$ (GeV)	L (km)	#CC $\nu$ /kt/yr
<b>K2K</b>	<b>1.3</b>	<b>250</b>	<b>2</b>
<b>NuMi (High E)</b>	<b>15</b>	<b>730</b>	<b>3100</b>
<b>NuMi (Low E)</b>	<b>3.5</b>	<b>730</b>	<b>469</b>
<b>CNGS</b>	<b>17.7</b>	<b>732</b>	<b>2448</b>
<b>JHF-I</b>	<b>0.7</b>	<b>295</b>	<b>133</b>
<b>Numi off-axis</b>	<b>2.3</b>	<b>820</b>	<b>~80</b>
<b>Super AGS</b>	<b>1.5</b>	<b>2540</b>	<b>11</b>
<b>JHF-II</b>	<b>0.7</b>	<b>295</b>	<b>691</b>
<b>SPL</b>	<b>0.26</b>	<b>130</b>	<b>16.3</b>
$\beta$ <b>beam**</b>	<b>0.58</b>	<b>130</b>	<b>84</b>

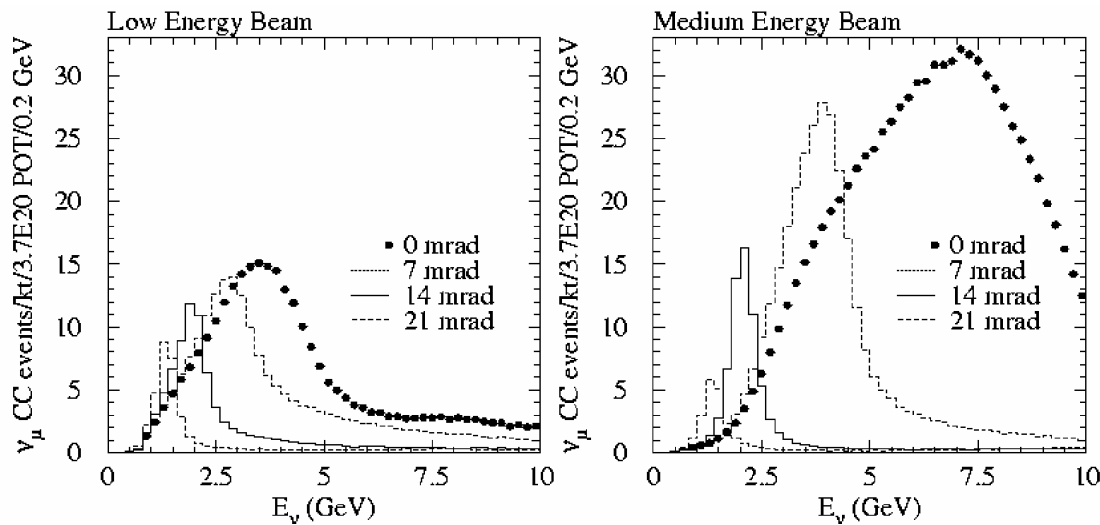
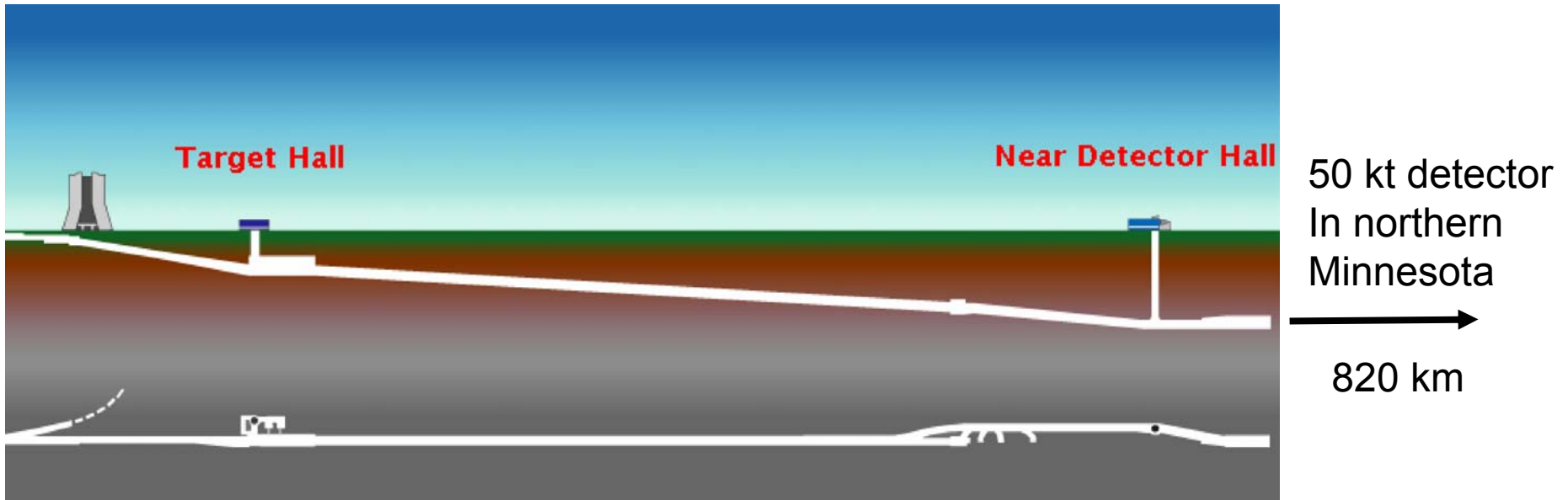
} R&D

# T2K Experimental Layout



Neutrino energy will be tuned between 0.4 and 1.0 GeV corresponding to:  $\delta m^2$  from 1.6 to  $4.0 \times 10^{-3} \text{ eV}^2$  to cover  $\delta m^2_{\text{ATM}}$  range.

# NuMI Beam



Beam energy can be varied.

# Matter Effects

If we now include matter effects:

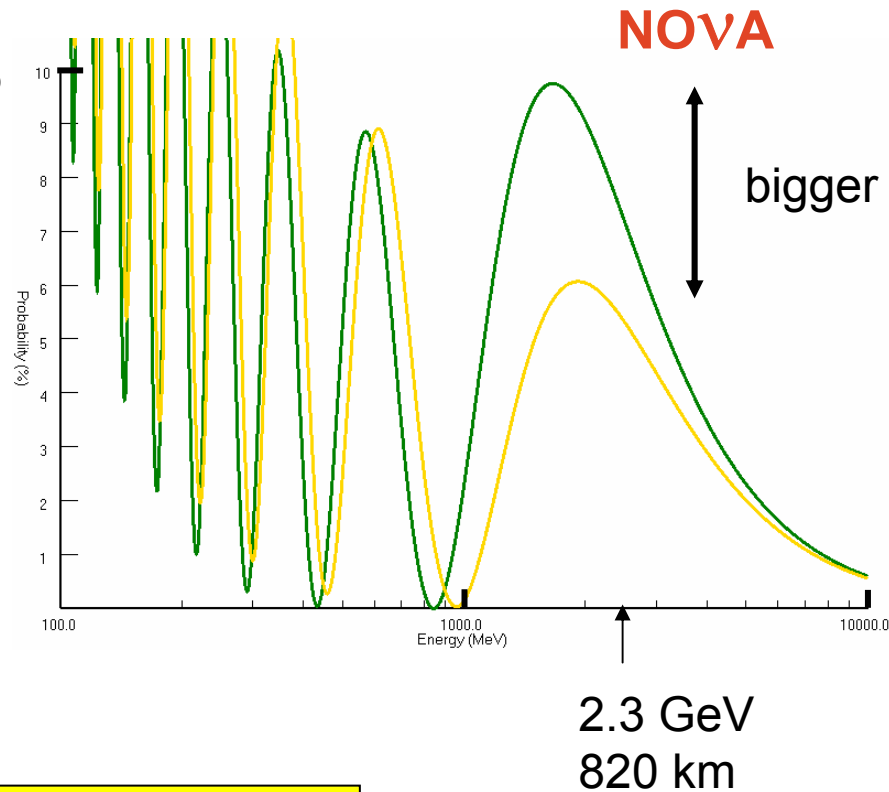
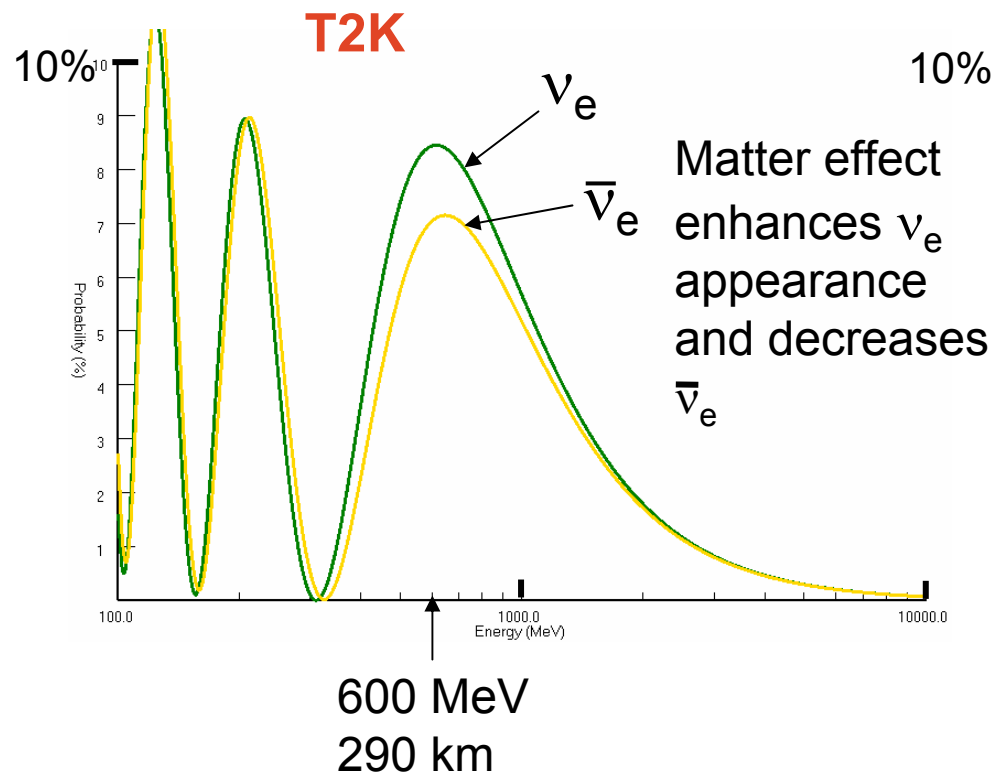
$$P_{\text{matt}\pm}[\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)] \Rightarrow \begin{matrix} \pm \cos 2\theta_{13} \sin^2 2\theta_{13} s_{23}^2 \left( \frac{2Ea(x)}{\Delta m_{13}^2} \right) \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right) \\ \mp \frac{a(x)L}{4} \sin^2 2\theta_{13} \cos 2\theta_{13} s_{23}^2 \sin \left( \frac{\Delta m_{13}^2 L}{2E} \right), \end{matrix}$$

$\nu$ 's  $\swarrow$   
 $\searrow$

Where  $a(x) = \sqrt{2}G_F N_e(x)$  ← Electron number density at x

- Matter induced effects are a function of  $E_\nu$  and can be large for long path lengths.
  - T2K ~10%
  - Nova ~25% (higher energy and longer distance)
- Opposite sign
  - for  $\nu$  and  $\bar{\nu}$
  - for NH and IH

# $\nu_e(\bar{\nu}_e)$ Prob. vs. Energy at CHOOZ Limit

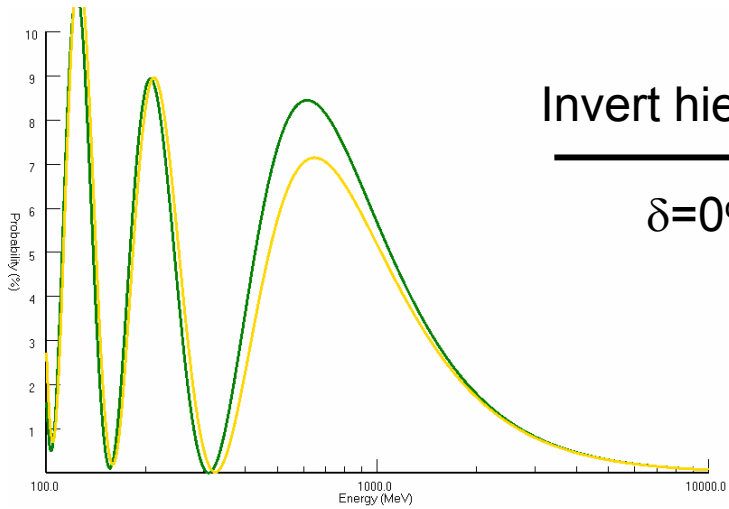


$$\delta m_{23}^2 = 2.5 \times 10^{-3} \text{ eV}^2 \quad \sin^2 2\theta_{23} = 1.0$$

$$\delta m_{12}^2 = 7.1 \times 10^{-5} \text{ eV}^2 \quad \sin^2 2\theta_{12} = 0.81$$

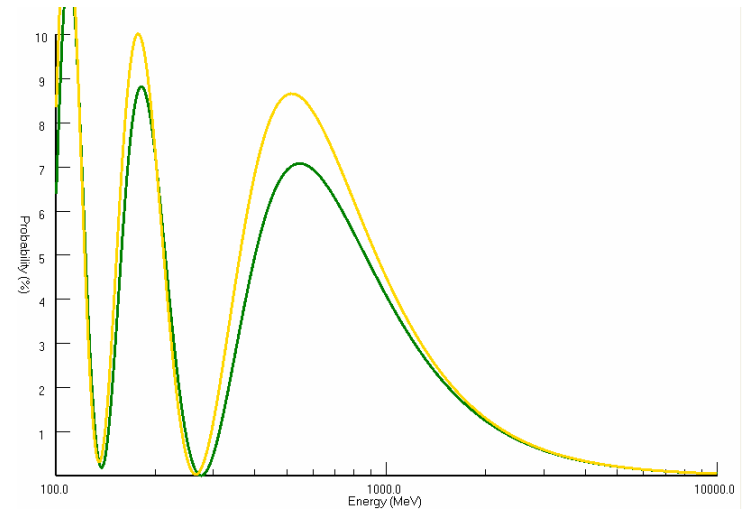
$$\sin^2 2\theta_{13} = 0.16$$

# Hierarchy/CP Degeneracy



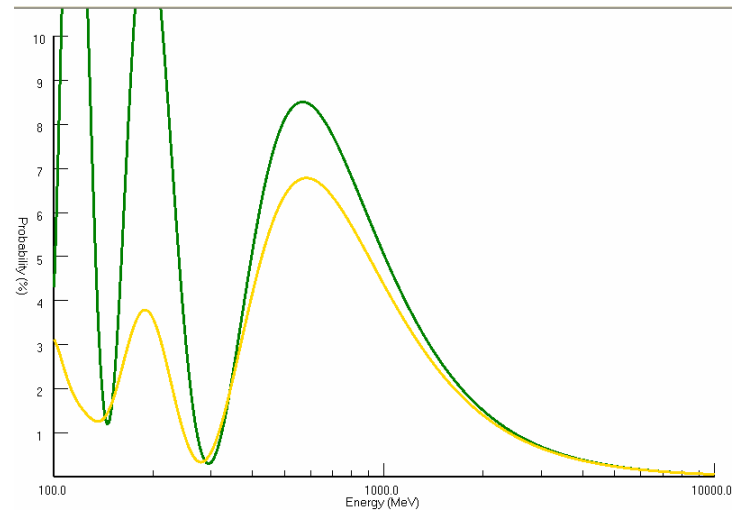
Invert hierarchy

$$\delta=0^\circ$$



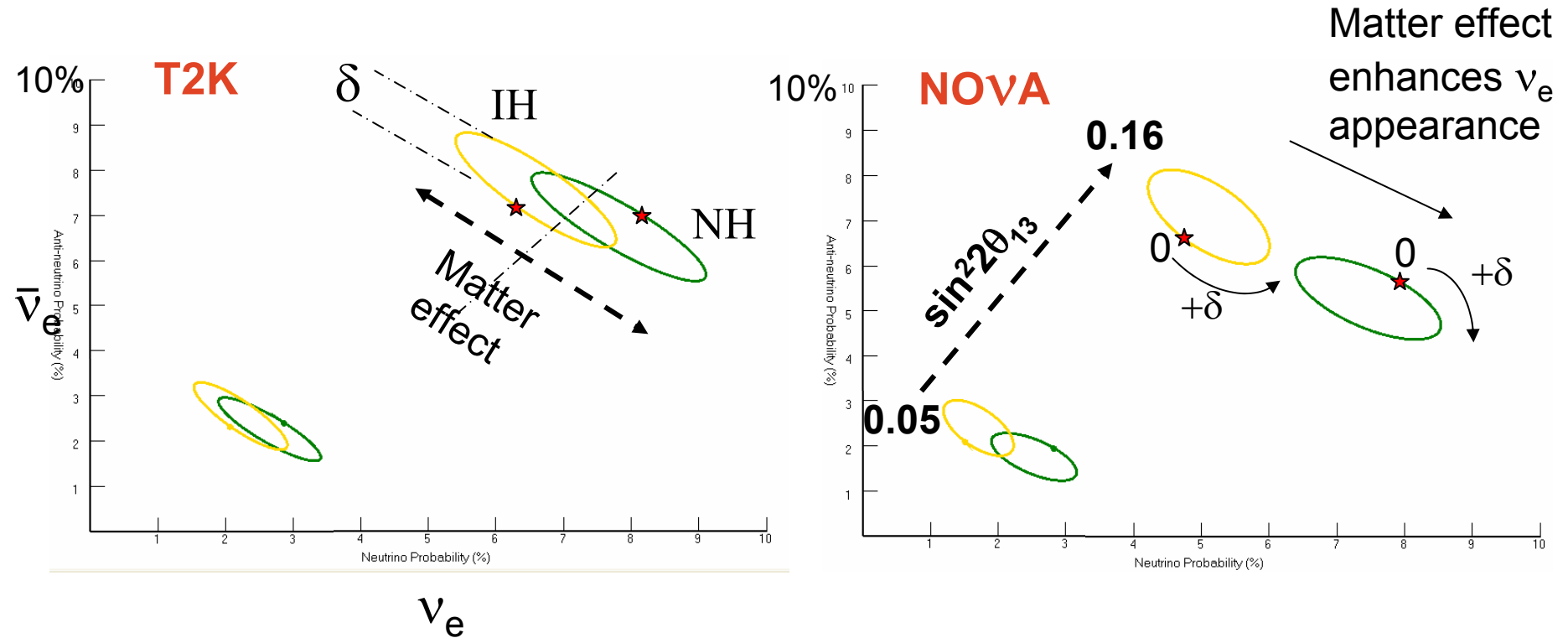
Invert hierarchy

$$\delta=-90^\circ$$



# $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ vs. $P(\nu_\mu \rightarrow \nu_e)$

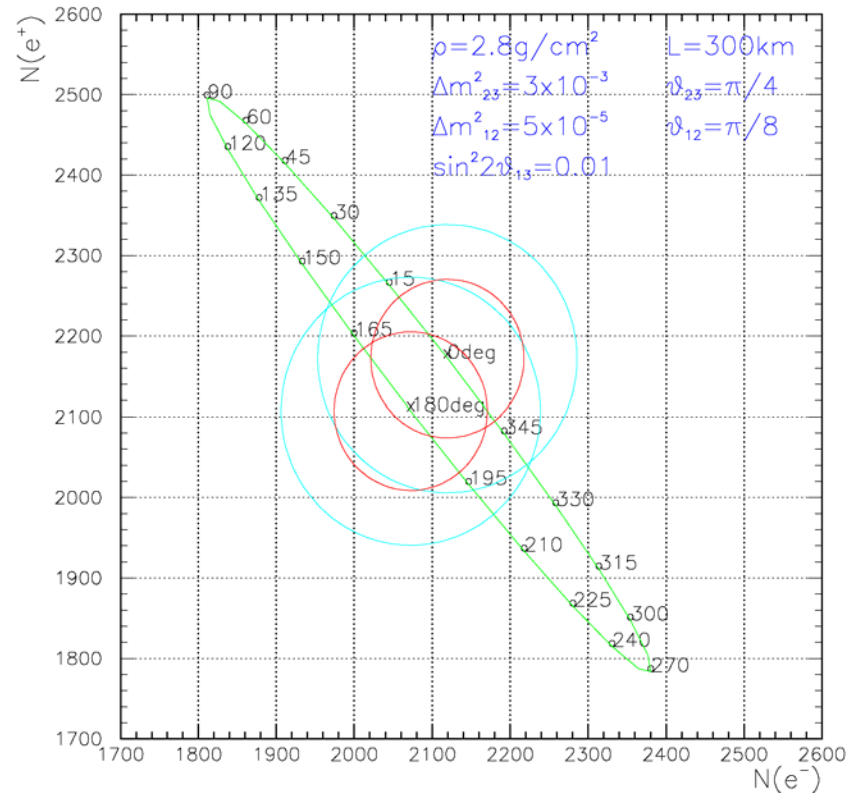
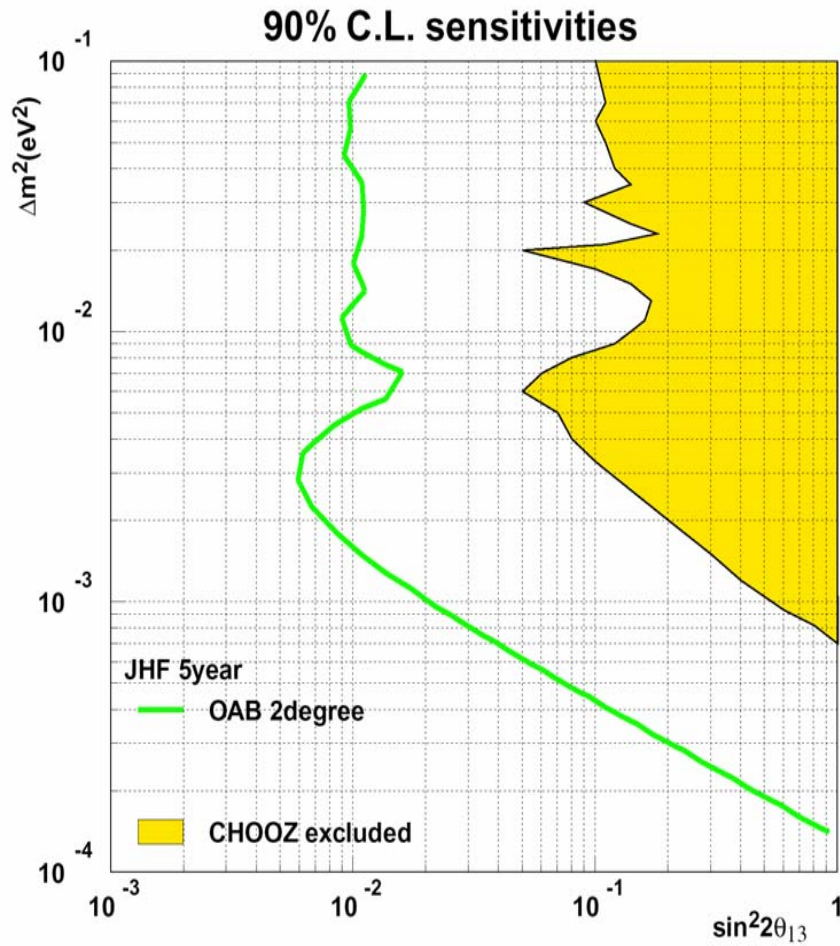
Minakata & Nunokawa hep-ph/0108085



$$\delta m^2_{23} = 2.5 \times 10^{-3} \text{ eV}^2 \quad \sin^2 2\theta_{23} = 1.0$$

$$\delta m^2_{12} = 7.1 \times 10^{-5} \text{ eV}^2 \quad \sin^2 2\theta_{12} = 0.81$$

# T2K Sensitivity

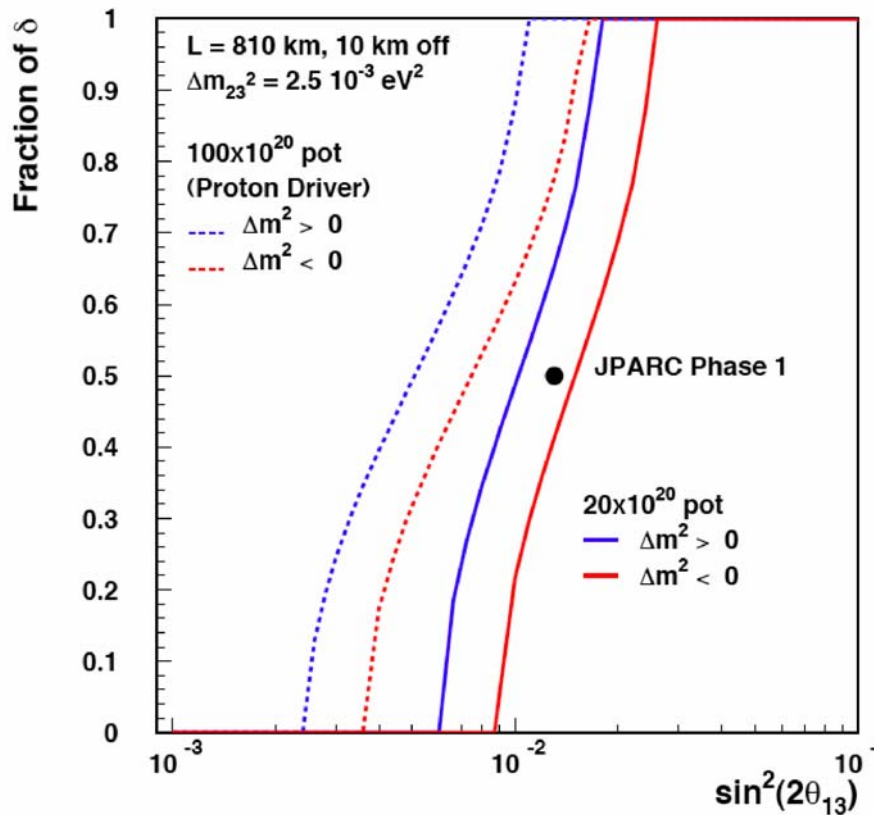


2 years  $\nu_\mu$ , 6 years  $\bar{\nu}_\mu$

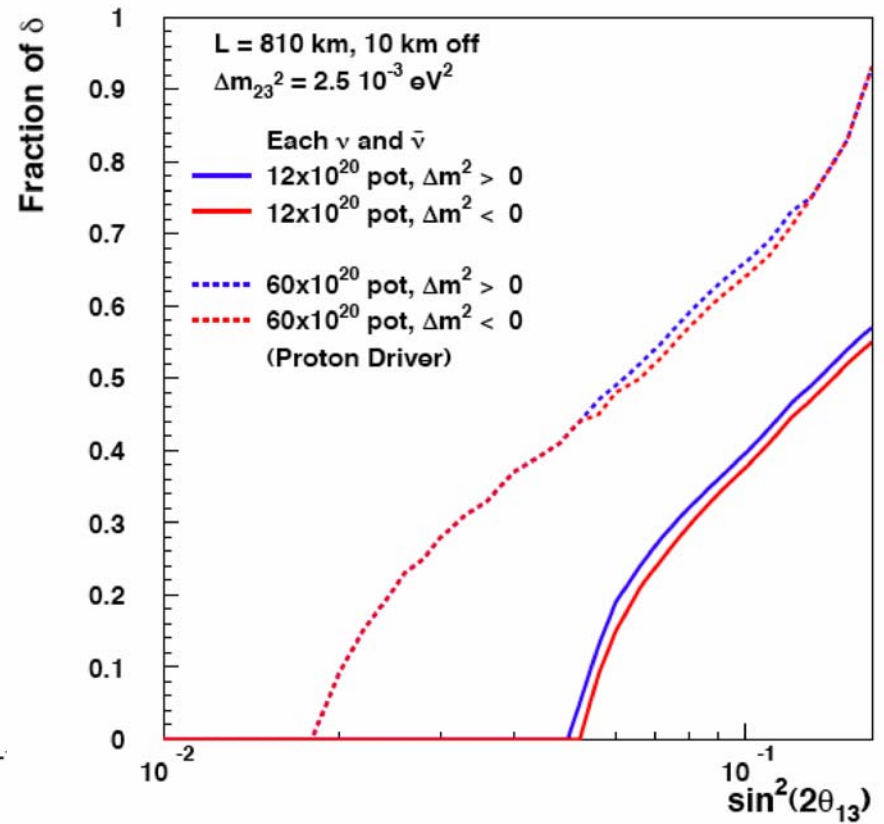
$3\sigma$  discovery possible if  $|\delta| > 20^\circ$

# NO $\nu$ A Sensitivity

3  $\sigma$  Sensitivity to  $\sin^2(2\theta_{13})$



2  $\sigma$  Resolution of the Mass Hierarchy

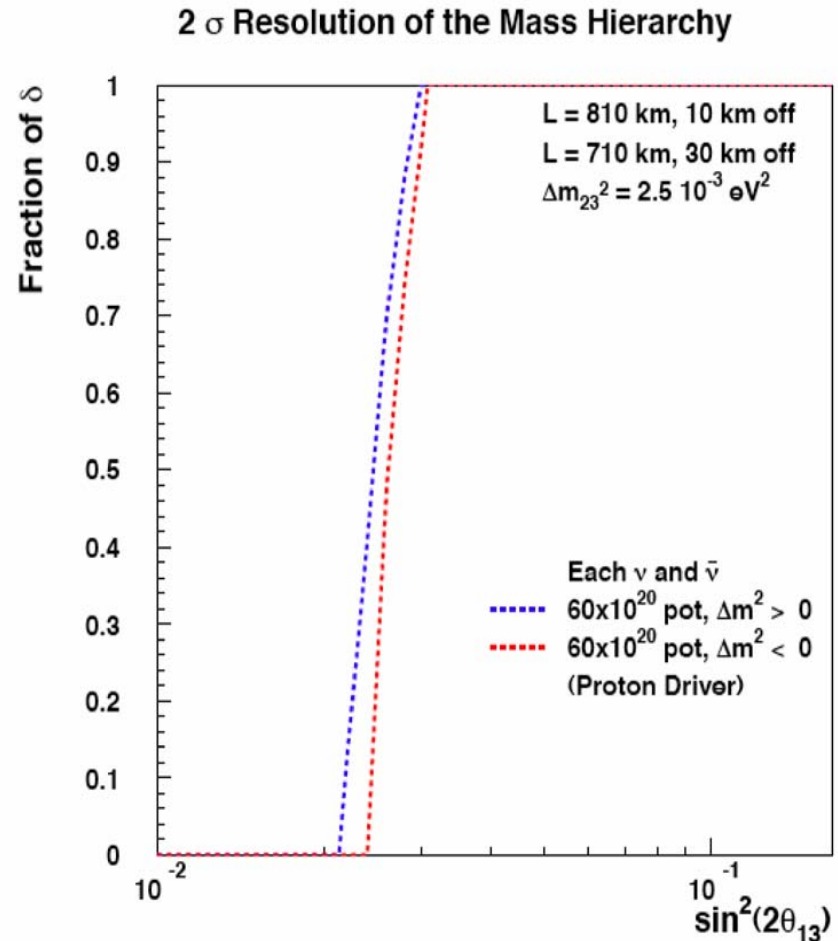


# Do Better On Hierarchy Resolution

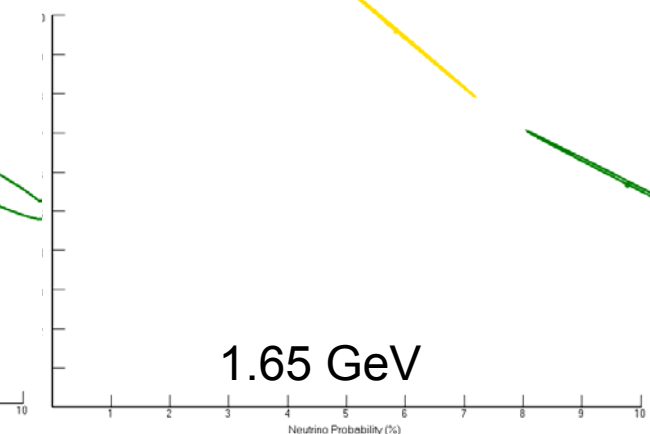
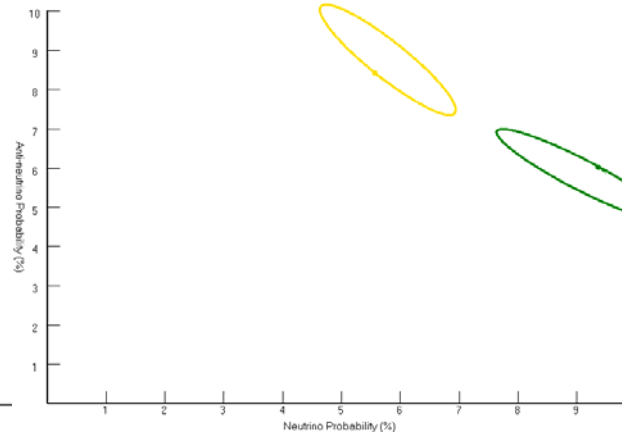
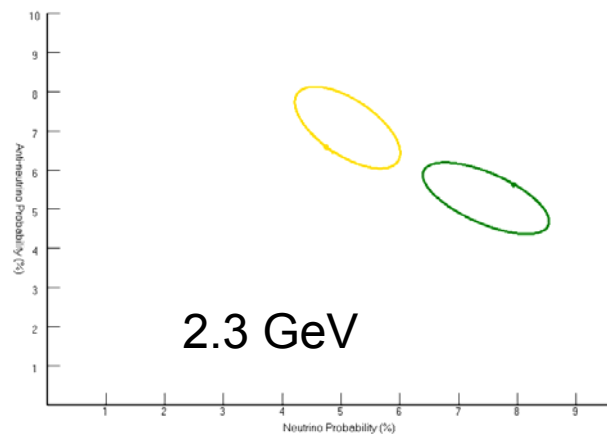
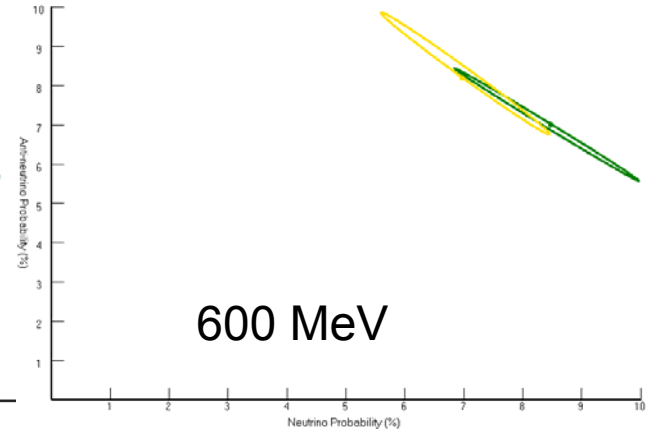
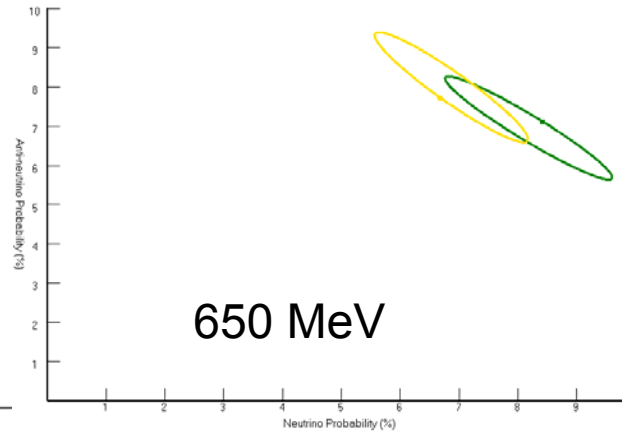
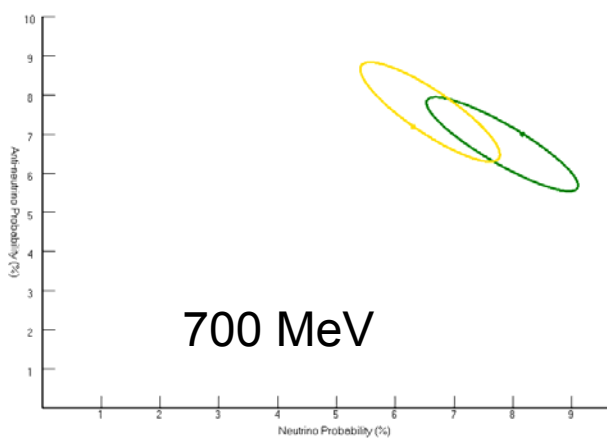
NOvA study:

Two Far Detectors Different Energies

Optimization under study



# Eliminate $\delta$ Uncertainty



Tune to oscillation maximum and measure with  $\nu$  and  $\bar{\nu}$

Hep-ph/0112345

# Summary

The off-axis technique is a very promising method to:

- discover if  $\theta_{13}$  is non-zero by observing  $\nu_e$  appearance
- enable high precision measurements of  $\theta_{23}$  and  $\delta m^2_{23}$
- More studies are needed to optimize the procedure for establishing the mass hierarchy and for searching for non-zero CP phase.
- Most likely several complimentary techniques will have to be used.
  - Different distances
  - Neutrino and anti-neutrino beams
  - Reactor measurements of  $\theta_{13}$